



LECTURE VIRTUAL MEMORY (CHAPTER 9)

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References

- *The slides here are adapted/modified from the textbook and its slides:
Operating System Concepts, Silberschatz et al., 7th & 8th editions, Wiley.*

REFERENCES

- Operating System Concepts, 7th and 8th editions, Silberschatz et al. Wiley.
- Modern Operating Systems, Andrew S. Tanenbaum, 3rd edition, 2009.

Outline

- Background
- Demand Paging
- Copy-on-Write
- Page Replacement
- Allocation of Frames
- Thrashing
- Memory-Mapped Files
- Allocating Kernel Memory
- Other Considerations
- Operating-System Examples

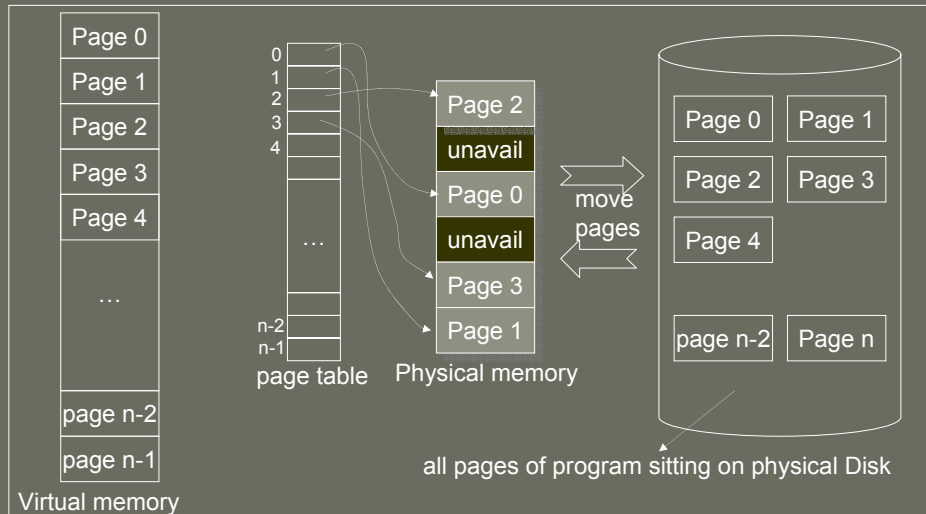
Objectives

- To describe the **benefits** of a virtual memory system
- To explain the concepts of **demand paging**, **page-replacement** algorithms, and **allocation of page frames**
- To discuss the principle of the **working-set** model

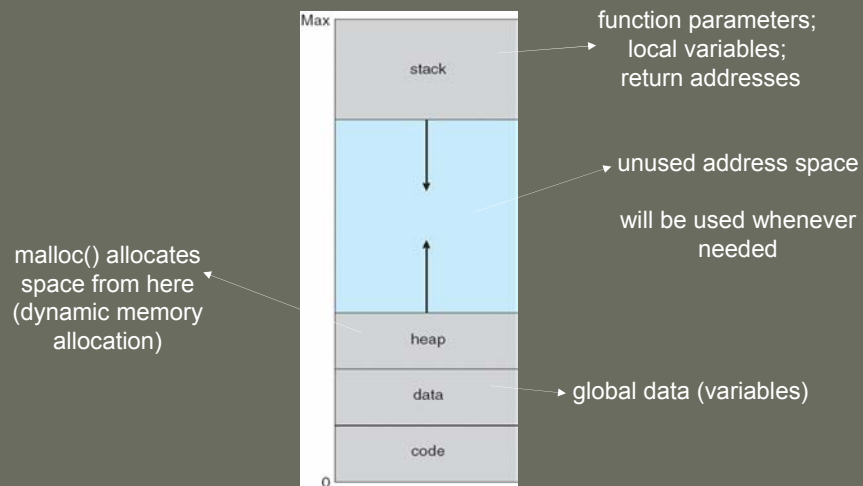
Background

- **Virtual memory** – separation of user logical memory from physical memory.
- Benefits:
 - Only **part of the program** needs to be in memory for execution
 - You can execute more programs concurrently
 - Logical address space can therefore be much larger than physical address space
 - You can execute programs larger than physical memory
 - Allows address spaces to be shared by several processes
 - Library or memory segment can be shared
 - Allows for more efficient process creation

Virtual Memory That is Larger Than Physical Memory



A typical virtual-address space layout of a process



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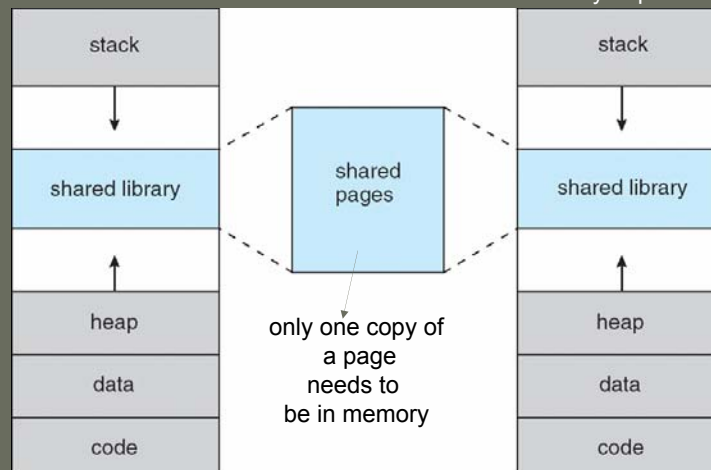
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Shared Library Using Virtual Memory

Virtual memory of process A

Virtual memory of process B



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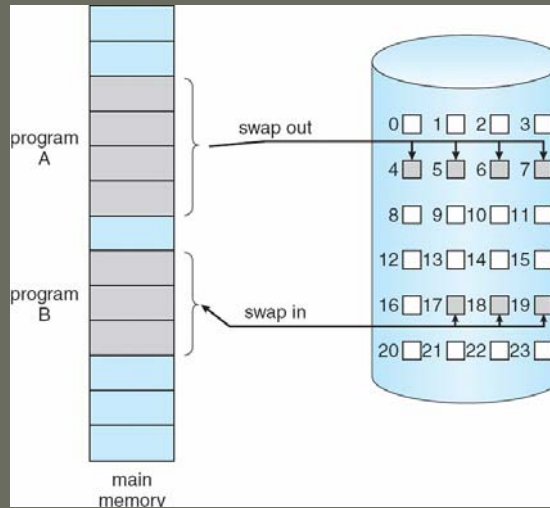
Implementing Virtual Memory

- Virtual memory can be implemented via:
 - **Demand paging**
 - Bring pages into memory when they are used, i.e. allocate memory for pages when they are used
 - **Demand segmentation**
 - Bring segments into memory when they are used, i.e. allocate memory for segments when they are used.

Demand Paging

- Bring a page into memory only when it is needed
 - Less I/O needed
 - Less memory needed
 - Faster response
 - More users
- Page is needed $\Rightarrow$ reference to it
 - invalid reference $\Rightarrow$ abort
 - not-in-memory $\Rightarrow$ bring to memory
- **Lazy swapper** – never swaps a page into memory unless page will be needed
 - Swapper that deals with pages is a **pager**

Transfer of a Paged Memory to Contiguous Disk Space



Valid-Invalid Bit

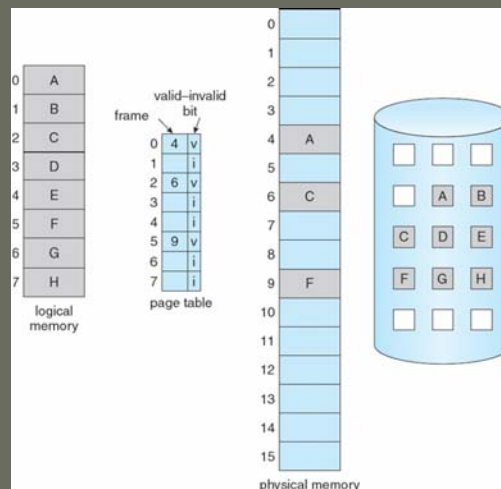
- With each page table entry a valid-invalid bit is associated (**v** $\Rightarrow$ in-memory, **i** $\Rightarrow$ not-in-memory)
- Initially valid-invalid bit is set to **i** on all entries
- Example of a page table snapshot:

Frame #	valid-invalid bit
	v
	v
	v
	v
	i
....	
	i
	i

page table

- During address translation, if valid-invalid bit in page table entry is **i** $\Rightarrow$ page fault

Page Table When Some Pages Are Not in Main Memory



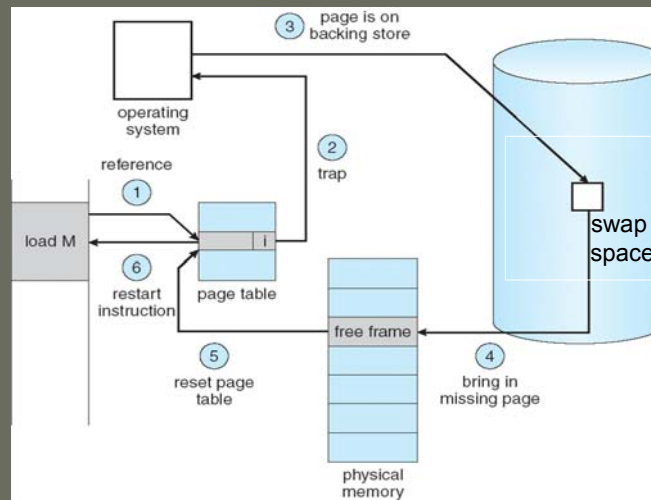
Page Fault

- While CPU is executing an instruction or trying to fetch an instruction: if there is a reference to a page, *first* reference to that page will trap to operating system (since page will not be in memory): this is called **page fault**

Page fault handling steps by OS:

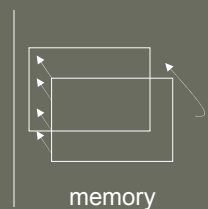
- Operating system looks at another table to decide:
 - Invalid reference (page is in *unused* portion of address space) $\Rightarrow$ abort
 - Just not in memory (page is in used portion, but not in RAM)
- Get empty frame
(we may need to remove a page; if removed page is modified, we need disk I/O to swap it out)
- Swap page into frame
(we need disk I/O)
- Reset tables (install mapping into page table)
- Set validation bit = **v**
- Restart the instruction that caused the page fault

Steps in Handling a Page Fault



Page Fault (Cont.)

- If page fault occur when trying to fetch an instruction, fetch the instruction again after bringing the page in.
- If page fault occurs while we are executing an instruction: Restart the instruction after bringing the page in.
- For most instructions, restarting the instruction is no problem.
- But for some, we need to be careful. Example:
 - block move instruction



Performance of Demand Paging

- Page Fault Rate $0 \leq p \leq 1.0$
 - if $p = 0$ no page faults
 - if $p = 1$, every reference is a fault
- Effective Access Time to Memory (EAT)

$$\begin{aligned} \text{EAT} = & (1 - p) \times \text{memory access} \\ & + p (\text{page fault overhead} \\ & \quad + \text{swap page out} \\ & \quad + \text{swap page in} \\ & \quad + \text{restart overhead} \\ &) \end{aligned}$$

Demand Paging Example

- Memory access time = 200 nanoseconds
- Average page-fault service time = 8 milliseconds
- $\text{EAT} = (1 - p) \times 200 + p (8 \text{ milliseconds})$
 $= (1 - p) \times 200 + p \times 8,000,000$
 $= 200 + p \times 7,999,800$
- If one access out of 1,000 causes a page fault ($p = 1/1000$), then
EAT = 8.2 microseconds.

This is a slowdown by a factor of 40!!
(200 ns / 8.2 microsec $\approx$ 1/40)

Process Creation

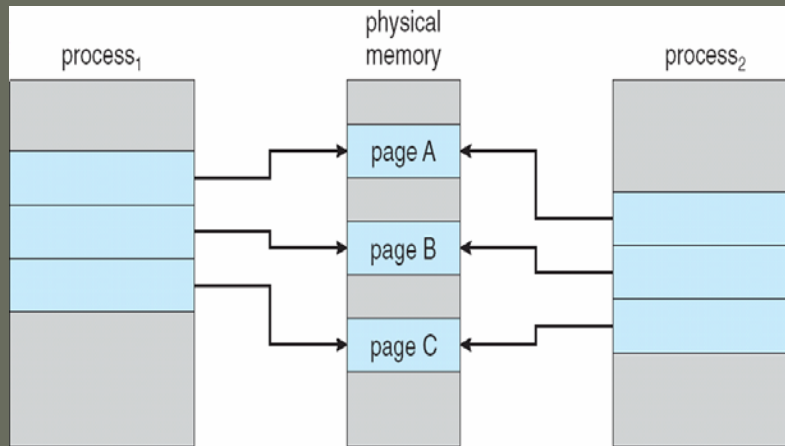
- Virtual memory allows other benefits during process creation:
 - Copy-on-Write
 - Memory-Mapped Files (later)

Copy-on-Write

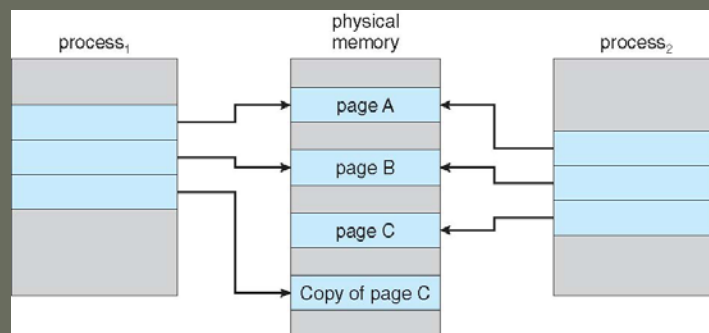
- Copy-on-Write (COW) allows both parent and child processes to initially *share* the same pages in memory

If either process modifies a shared page, only then is the page copied
- COW allows more efficient process creation as only modified pages are copied

Before Process 1 Modifies Page C



After Process 1 Modifies Page C



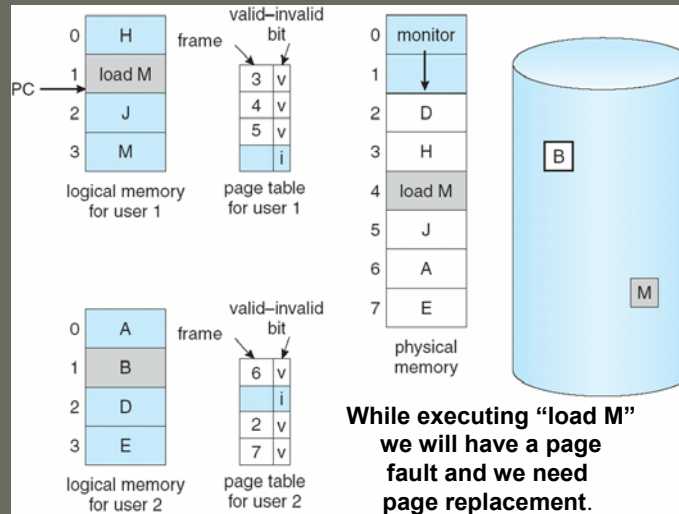
What happens if there is no free frame?

- **Page replacement** – find some page in memory, but not really in use, swap it out
 - Algorithm ? Which page should be remove?
 - performance – want an algorithm which will result in minimum number of page faults
- With page replacement, same page may be brought into memory several times

Page Replacement

- **Prevent over-allocation** of memory by modifying page-fault service routine to include page replacement
- Use **modify (dirty) bit** to reduce overhead of page transfers – only modified pages are written to disk while removing/replacing a page.
- Page replacement completes separation between logical memory and physical memory
 - large virtual memory can be provided on a smaller physical memory

Need For Page Replacement

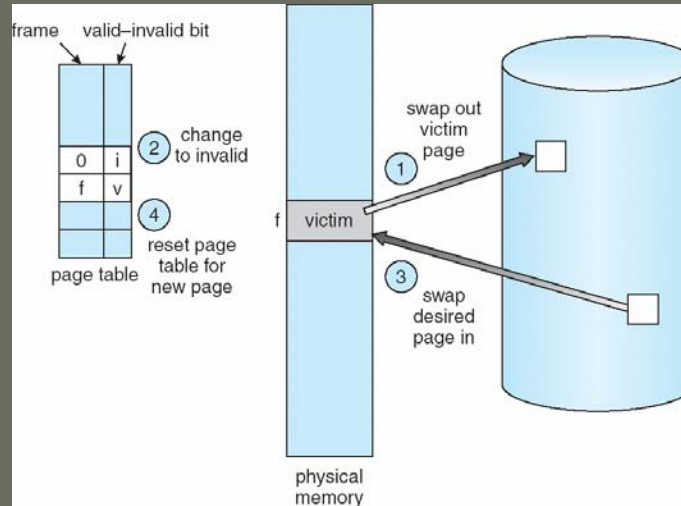


Basic Page Replacement

Steps performed by OS while replacing a page upon a page fault:

1. Find the location of the desired page on disk
2. Find a free frame:
 - If there is a free frame, use it
 - If there is no free frame, use a page replacement algorithm to select a **victim** frame; if the victim page is modified, write it back to disk.
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Restart the process

Page Replacement



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Page Replacement Algorithms

- Want lowest page-fault rate
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
- In all our examples, the reference string is

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

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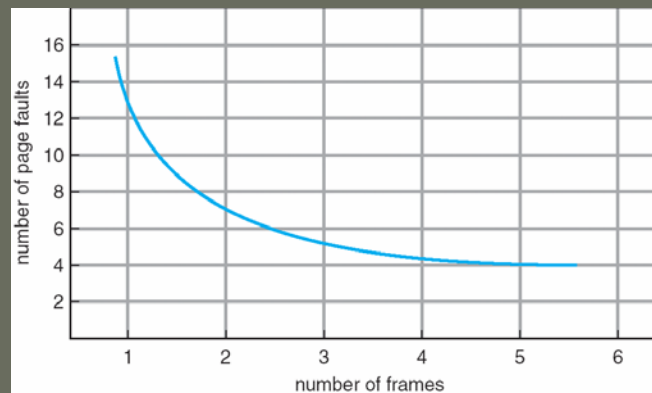
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Driving reference string

- Assume process makes the following memory references in a system with 100 bytes per page:
0100 0432 0101 0612 0102 0103 0104 0101 0611 0102 0103 0104
0101 0610 0102 0103 0104 0609 0102 0105
- Pages referenced with each memory reference
 - 0, 4, 1, 6, 1, 1, 1, 1, 6, 1, 1, 1, 6, 1, 1, 6, 1, 1
- Corresponding page reference string
 - 0, 4, 1, 6, 1, 6, 1, 6, 1, 6, 1

Graph of Page Faults Versus The Number of Frames



First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 3 frames (3 pages can be in memory at a time per process)

1	1	4	5
2	2	1	3
3	3	2	4

9 page faults

- 4 frames

1	1	5	4
2	2	1	5
3	3	2	
4	4	3	

10 page faults

- Belady's Anomaly: more frames $\Rightarrow$ more page faults

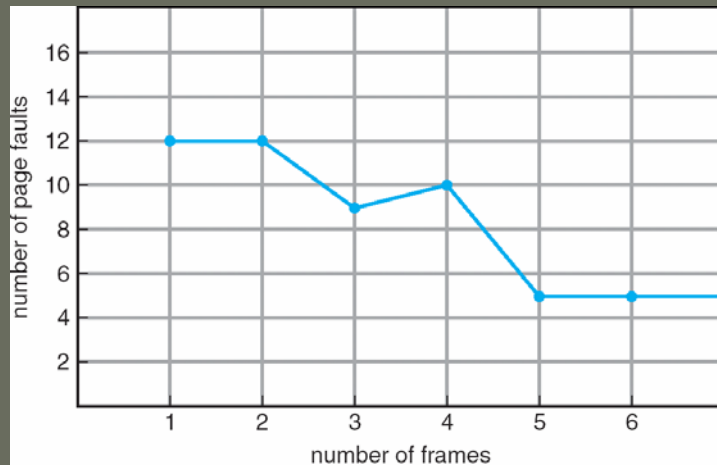
FIFO Page Replacement

reference string

7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
7	7	7	2		2	2	4	4	4	0			0	0			7	7	7
	0	0	0		3	3	3	2	2	2			1	1			1	0	0
		1	1		1	0	0	0	3	3			3	2			2	2	1

page frames

FIFO Illustrating Belady's Anomaly



Optimal Algorithm

- Replace page that will not be used for longest period of time
- 4 frames example

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

1
2
3
4

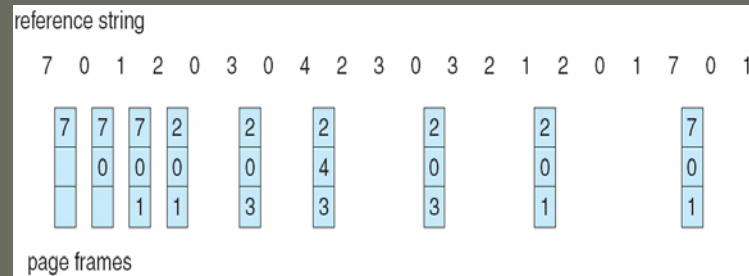
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6 page faults

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- How do you know this?
- Used for measuring how well your algorithm performs

Optimal Page Replacement



Least Recently Used (LRU) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, **5**, 1, 2, **3**, **4**, **5**

1	1	1	1	5
2	2	2	2	2
3	5	5	4	4
4	4	3	3	3

8 page faults

LRU Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0		1		1		1			
	0	0	0		0		0	0	3	3		3		0		0			
		1	1		3		3	2	2	2		2		2		7			

page frames

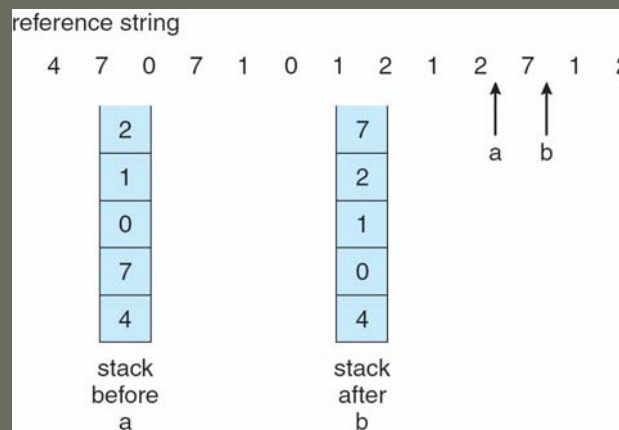
LRU Algorithm Implementation

- **Counter** implementation
 - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
 - When a page needs to be replaced, look at the counters to determine which one to replace
 - The one with the smallest counter value will be replaced

LRU Algorithm Implementation

- **Stack** implementation – keep a stack of page numbers in a double link form:
 - Page referenced:
 - move it to the top
 - requires 6 pointers to be changed (with every memory reference; costly)
 - No search for replacement (replacement fast)

Use of a Stack to Record The Most Recent Page References

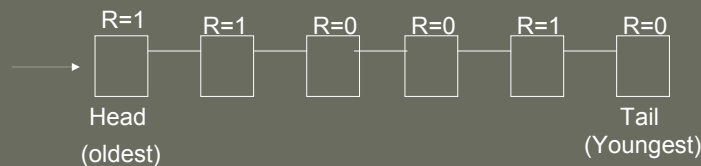


LRU Approximation Algorithms

- Reference bit
 - With each page associate a bit, initially = 0 (not referenced/used)
 - When page is referenced, bit set to 1
 - Replace the one which is 0 (if one exists)
 - We do not know the order, however (several pages may have 0 value)
 - Reference bits are cleared periodically (with every clock interrupt);

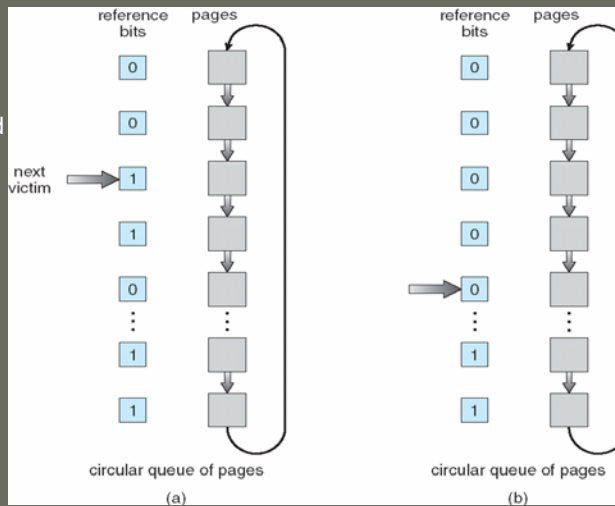
Second chance algorithm

- Second chance
 - FIFO that is checking if page is referenced or not
 - Need reference bit
 - If page to be replaced, look to the FIFO list; remove the page close to head of the list and that has reference bit 0.
 - If there is a page you encounter that has reference bit 1, move it to the back after clearing the reference bit. Try to find another page that has 0 as reference bit.
 - May require to change all 1's to 0's and then come back to the beginning of the queue.



Second-Chance (clock) Page-Replacement Algorithm

Second chance can be implemented using a circular list of pages; Then it is also called Clock algorithm



Counting Algorithms

- Keep a counter of the number of references that have been made to each page
- **LFU Algorithm:** replaces page with smallest count
- **MFU Algorithm:** based on the argument that the page with the smallest count was probably just brought in and has yet to be used

Allocation of Frames

- Each process needs *minimum* number of pages
- Example: IBM 370 – 6 pages to handle SS MOVE instruction:
 - instruction is 6 bytes, might span 2 pages
 - 2 pages to handle *from*
 - 2 pages to handle *to*
- Two major allocation schemes
 - fixed allocation
 - priority allocation

Fixed Allocation

- Equal allocation – For example, if there are 100 frames and 5 processes, give each process 20 frames.
- Proportional allocation – Allocate according to the size of process
 - s_i = size of process p_i
 - $S = \sum s_i$
 - m = total number of frames
 - a_i = allocation for $p_i = \frac{s_i}{S} \times m$

Example:

$$\begin{aligned}m &= 64 \\s_i &= 10 \\s_2 &= 127 \\a_1 &= \frac{10}{137} \times 64 \approx 5 \\a_2 &= \frac{127}{137} \times 64 \approx 59\end{aligned}$$

Priority Allocation

- Use a proportional allocation scheme using priorities rather than size
- If process P_i generates a page fault,
 - select for replacement one of its frames
 - select for replacement a frame from a process with lower priority number

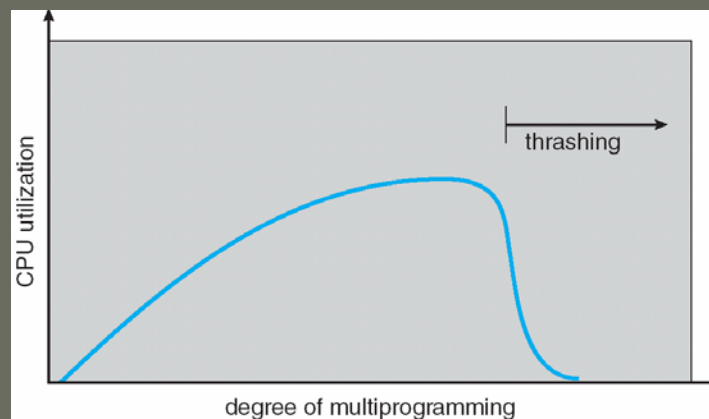
Global versus Local Allocation

- **Global replacement** – process selects a replacement frame from the set of all frames; one process can take a frame from another
- **Local replacement** – each process selects from only its own set of allocated frames

Thrashing

- If a process does not have “enough” pages, the **page-fault rate is very high**. This leads to:
 - low CPU utilization
 - operating system thinks that it needs to increase the degree of multiprogramming
 - another process added to the system
- **Thrashing** $\equiv$ a process is busy swapping pages in and out

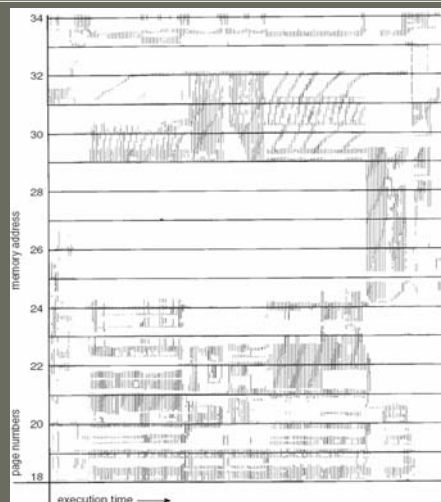
Thrashing (Cont.)



Demand Paging and Thrashing

- Why does demand paging work?
Locality model
 - Process migrates from one locality to another
 - Localities may overlap
- Why does thrashing occur?
 Σ size of locality > total memory size

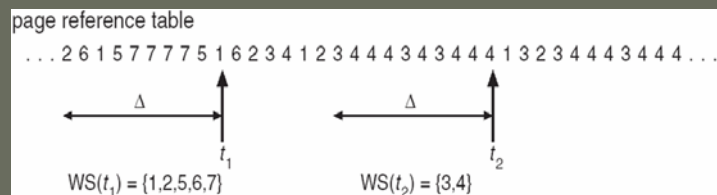
Locality In A Memory-Reference Pattern



Working-Set Model

- $\Delta \equiv$ working-set window $\equiv$ a fixed number of page references
Example: 10,000 instruction
- WSS_i (working set of Process P_i) =
total number of pages referenced in the most recent Δ (varies in time)
 - if Δ too small will not encompass entire locality
 - if Δ too large will encompass several localities
 - if $\Delta = \infty \Rightarrow$ will encompass entire program
- $D = \sum WSS_i \equiv$ total demand for frames
- if $D > m \Rightarrow$ Thrashing (m : #frames in memory)
- Policy if $D > m$, then suspend one of the processes

Working-Set Model



Keeping Track of Working-Set

	R_bit
x	0
y	0
y	0
w	0

page table

	additional ref_bits	
x	0	0
y	0	0
y	0	0
w	0	0

Physical Memory

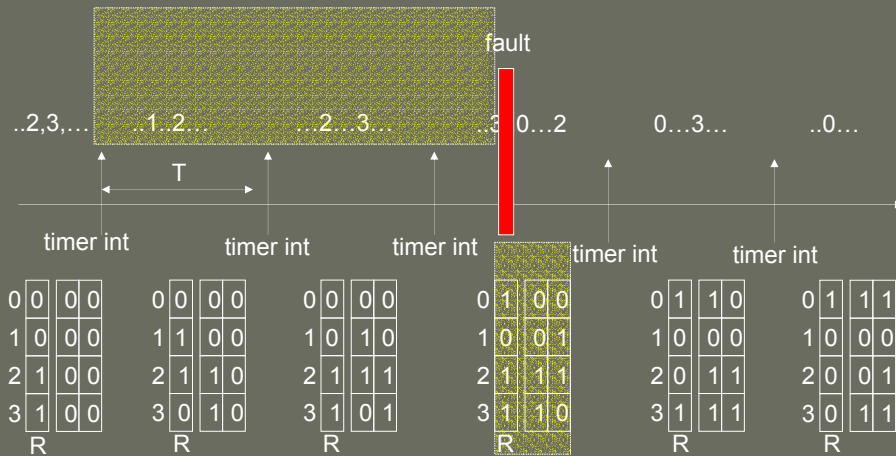
page x	frame 0
Page y	frame 1
Page z	frame 2
Page w	frame 3

Keeping Track of Working-Set

- Approximate with interval timer + a reference bit
- Example: $\Delta = 10,000$ (time units)
- Timer interrupts after every 5000 time units
- Keep in memory 2 bits for each page
- Whenever a timer interrupts copy and sets the values of all reference bits to 0
 - If one of the bits in memory = 1 $\Rightarrow$ page in working set
- Why is this not completely accurate?
 - Granularity is 5000 time_units (we don't know when exactly in it reference has occurred)
- Improvement = 10 bits and interrupt every 1000 time units.

Keeping Track of Working-Set (example)

$\Delta \approx 2T$



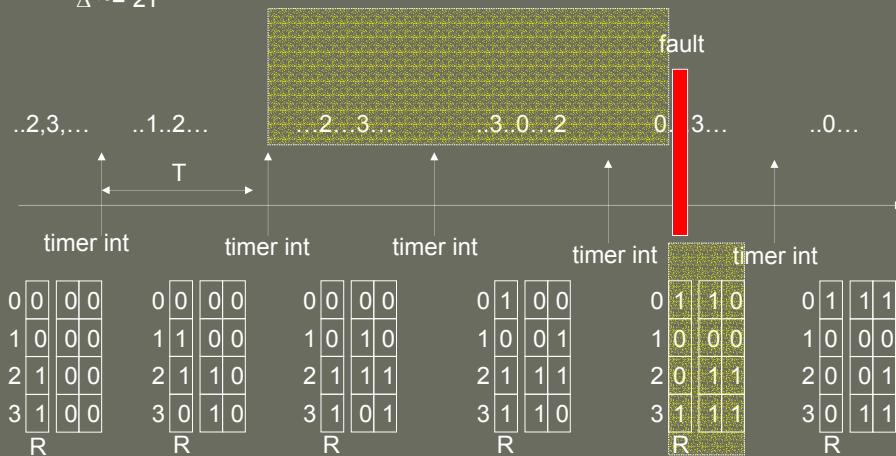
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Keeping Track of Working-Set (example continued)

$\Delta \approx 2T$



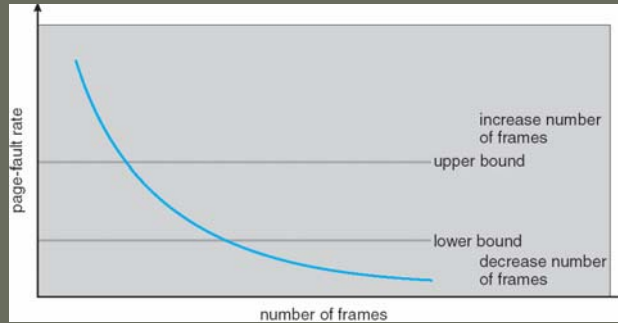
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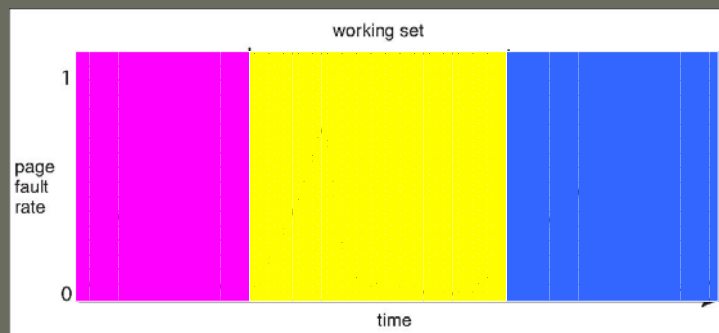
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Page-Fault Frequency (PFF) Scheme

- Establish “acceptable” page-fault rate
 - If actual rate too low, process loses frame
 - If actual rate too high, process gains frame



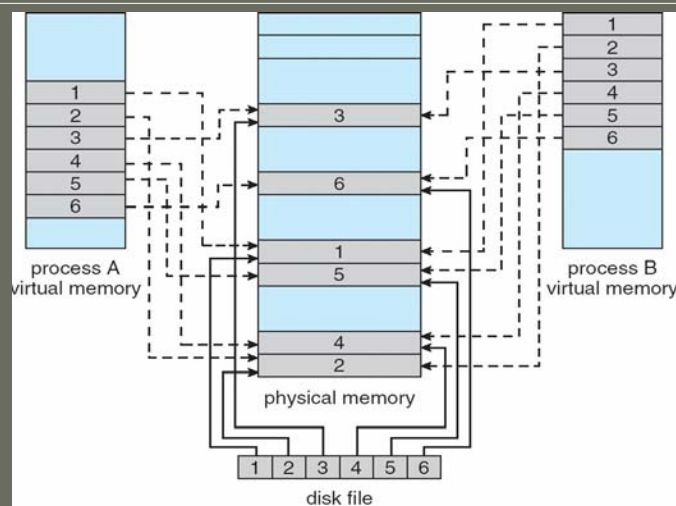
Working Sets and Page Fault Rates



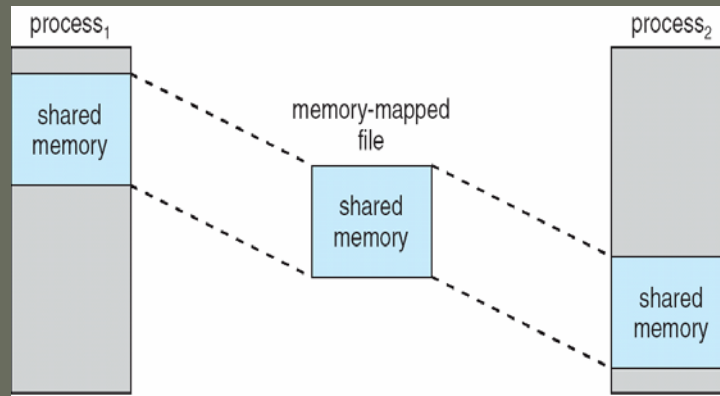
Memory-Mapped Files

- Memory-mapped file I/O allows file I/O to be treated as routine memory access by **mapping** a disk block to a page in memory
- A file is initially read using demand paging. A page-sized portion of the file is read from the file system into a physical page. Subsequent reads/writes to/from the file are treated as ordinary memory accesses.
- Simplifies file access by treating file I/O through memory rather than `read()` `write()` system calls
- Also allows several processes to map the same file allowing the pages in memory to be shared

Memory Mapped Files



Memory-Mapped Shared Memory in Windows



Allocating Kernel Memory

- Treated differently from user memory
- Often allocated from a free-memory pool
 - Kernel requests memory for structures (objects) of varying sizes
 - Process descriptors, semaphores, file objects,
 - Those structures have sizes much less than the page size
 - Some kernel memory needs to be contiguous
- This is dynamic memory allocation problem.
- But using first-fit like strategies (heap management strategies) cause external fragmentation

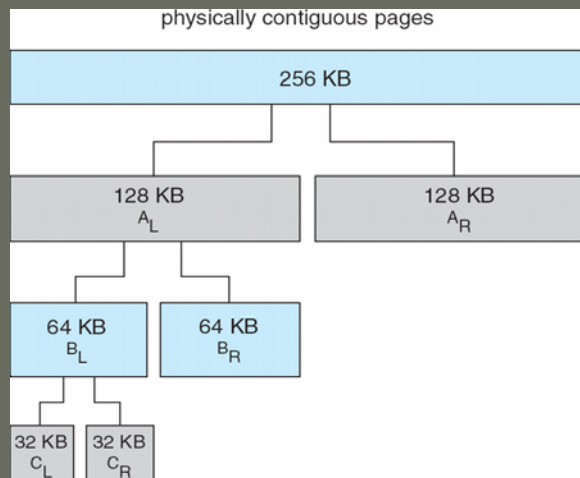
Allocating Kernel Memory

- We will see two methods
 - Buddy System Allocator
 - Slab Allocator

Buddy System Allocator

- Allocates memory from fixed-size segment consisting of physically-contiguous pages
- Memory allocated using **power-of-2 allocator**
 - Satisfies requests in units sized as power of 2
 - Request rounded up to next highest power of 2
 - When smaller allocation needed than is available, current chunk split into two buddies of next-lower power of 2
 - Continue until appropriate sized chunk available

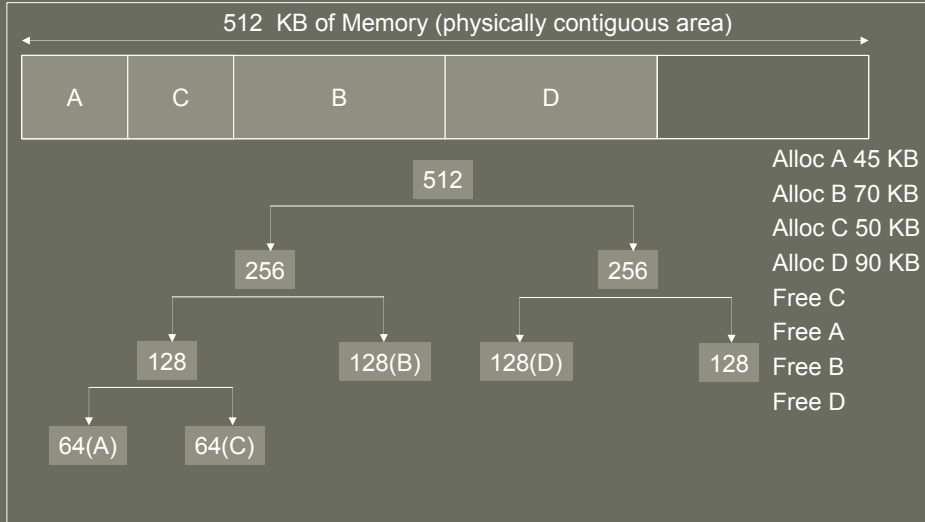
Buddy System Allocator



Example

- Object A needs memory 45 KB in size
- Object B needs memory 70 KB in size
- Object C needs memory 50 KB in size
- Object D needs memory 90 KB in size
- Object C removed
- Object A removed
- Object B removed
- Object D removed

Example



Slab Allocator

- Alternate strategy
- Within kernel, a considerable amount of memory is allocated for a finite set of objects such as process descriptors, file descriptors and other common structures
- Idea:
 - a contiguous phy memory (slab)
(a set of page frames)
 - a contiguous phy memory (slab)
(a set of page frames)

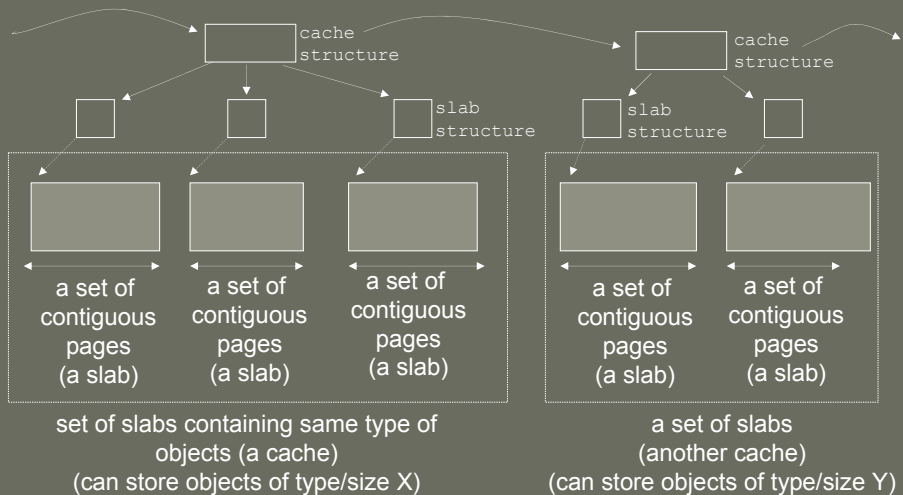


Obj X: object of type X
Obj Y: object of type Y

Slab Allocator

- **Slab** is one or more physically contiguous pages
- **Cache** consists of one or more slabs
- Single cache for each unique kernel data structure
 - Each cache filled with **objects** – instantiations of the data structure
- When cache created, filled with slots (objects) marked as **free**
- When structures stored, objects marked as **used**
- If slab is full of used objects, next object allocated from empty slab
 - If no empty slabs, new slab allocated
- Benefits include
 - no fragmentation,
 - fast memory request satisfaction

Slabs and Caches



Cache structure

- A set of slabs that contain one type of object is considered as a cache.
- Cache structure is a structure that keeps information about the cache and includes pointers to the slabs.

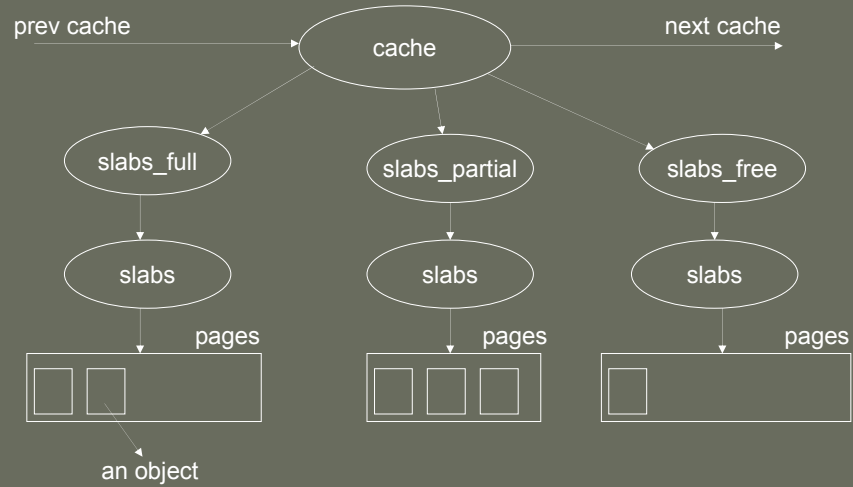
```
struct kmem_cache_s {
    struct list_head slabs_full; /* points to the full slabs */
    struct list_head slabs_partial; /* points to the partial slabs */
    struct list_head slabs_free; /* points to the free slabs */
    unsigned int objsize; /* size of objects stored in this cache */
    unsigned int flags;
    unsigned int num;
    spinlock_t spinlock;
    ...
    ...
}
```

Slab structure

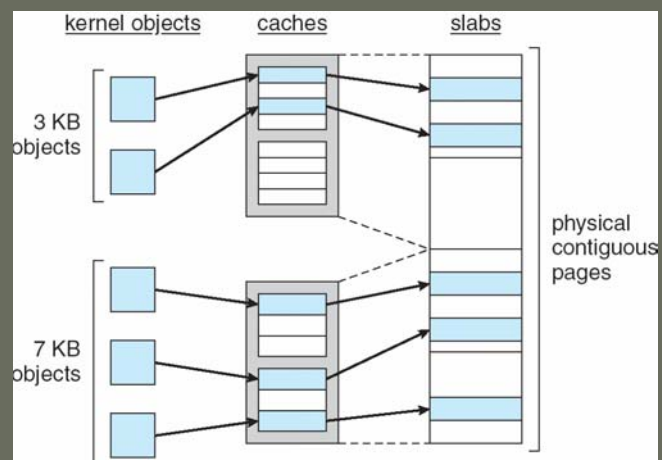
- A slab structure is a data structure that points to a contiguous set of page frames (a slab) that can store some number of objects of same size.
- A slab can be considered as a set of slots (slot size = object size). Each slot in a slab can hold one object.
- Which slots are free are maintained in the slab structure

```
typedef struct slab_s {
    struct list_head list;
    unsigned long colouroff;
    void *s_mem; /* start address of first object */
    unsigned int inuse; /* number of active objects */
    kmem_bufctl_t free; /* info about free objects */
} slab_t;
```

Layout of Slab Allocator



Slab Allocation



Slab Allocator in Linux

- `cat /proc/slabinfo` will give info about the current slabs and objects

→ cache names: one cache for each different object type

# name	<active>	<objs>	<num>	<objsize>	<objperslab>	<pagesperslab>	<limit>	<batchcount>	<sharedavail>
sharedfactor	slabdata	<active>	<slabs>	<num>	<slabs>	<sharedavail>			
ip_fib_alias	15	113	32	113	1	tunables	120	60	8 : slabdata 1 1 0
ip_fib_hash	15	113	32	113	1	tunables	120	60	8 : slabdata 1 1 0
dm_tio	0	0	16	203	1	tunables	120	60	8 : slabdata 0 0 0
dm_io	0	0	20	169	1	tunables	120	60	8 : slabdata 0 0 0
uhci_urb_priv	4	127	28	127	1	tunables	120	60	8 : slabdata 1 1 0
jbd_4k	0	0	4096	1	1	tunables	24	12	8 : slabdata 0 0 0
ext3_inode_cache	128604	128696	504	8	1	tunables	54	27	8 : slabdata 16087 16087 0
ext3_xattr	24084	29562	48	78	1	tunables	120	60	8 : slabdata 379 379 0
journal_handle	16	169	20	169	1	tunables	120	60	8 : slabdata 1 1 0
journal_head	75	144	52	72	1	tunables	120	60	8 : slabdata 2 2 0
revoke_table	2	254	12	254	1	tunables	120	60	8 : slabdata 1 1 0
revoke_record	0	0	16	203	1	tunables	120	60	8 : slabdata 0 0 0
scsi_cmd_cache	35	60	320	12	1	tunables	54	27	8 : slabdata 5 5 0
...									
files_cache	104	170	384	10	1	tunables	54	27	8 : slabdata 17 17 0
signal_cache	134	144	448	9	1	tunables	54	27	8 : slabdata 16 16 0
sighand_cache	126	126	1344	3	1	tunables	24	12	8 : slabdata 42 42 0
task_struct	179	195	1392	5	2	tunables	24	12	8 : slabdata 39 39 0
anon_vma	2428	2540	12	254	1	tunables	120	60	8 : slabdata 10 10 0
pgd	89	89	4096	1	1	tunables	24	12	8 : slabdata 89 89 0
pid	170	303	36	101	1	tunables	120	60	8 : slabdata 3 3 0

active objects

size

Prepaging

- Prepaging
 - To reduce the large number of page faults that occurs at process startup
 - Prepage all or some of the pages a process will need, before they are referenced
 - But if prepagged pages are unused, I/O and memory was wasted
 - Assume s pages are prepagged and α of the pages is used
 - Is cost of $s * \alpha$ save pages faults > or < than the cost of prepagging $s * (1 - \alpha)$ unnecessary pages?
 - α near zero $\Rightarrow$ prepagging loses

Other Issues – Page Size

- Page size selection must take into consideration:
 - **Fragmentation**
 - Small page size reduces fragmentation
 - **table size**
 - Large page size reduces page table size
 - **I/O overhead**
 - Large page size reduce I/O overhead (seek time, rotation time)
 - **Locality**
 - Locality is improved with smaller page size.

Other Issues – TLB Reach

- TLB Reach - The amount of memory accessible from the TLB
- $\text{TLB Reach} = (\text{TLB Size}) \times (\text{Page Size})$
- Ideally, the working set of each process is stored in the TLB
 - Otherwise there is a high degree of page faults
- Increase the Page Size
 - This may lead to an increase in fragmentation as not all applications require a large page size
- Provide Multiple Page Sizes
 - This allows applications that require larger page sizes the opportunity to use them without an increase in fragmentation

Other Issues – Program Structure

- Program structure
 - `int[128,128] data;`
 - Each row is stored in one page assuming `pagesize=512` bytes
- | | | | | | |
|----------|-----|-----|-----|--|-----|
| page 0 | int | int | int | | int |
| Page 1 | int | int | int | | int |
| | | | | | |
| Page 127 | int | int | int | | int |
- Program 1

```

for (j = 0; j < 128; j++)
    for (i = 0; i < 128; i++)
        data[i,j] = 0;
      
```

128 x 128 = 16,384 page faults
- Program 2

```

for (i = 0; i < 128; i++)
    for (j = 0; j < 128; j++)
        data[i,j] = 0;
      
```

128 page faults

Other Issues – I/O interlock

- **I/O Interlock** – Pages must sometimes be locked into memory
- Consider I/O - Pages that are used for copying a file from a device must be